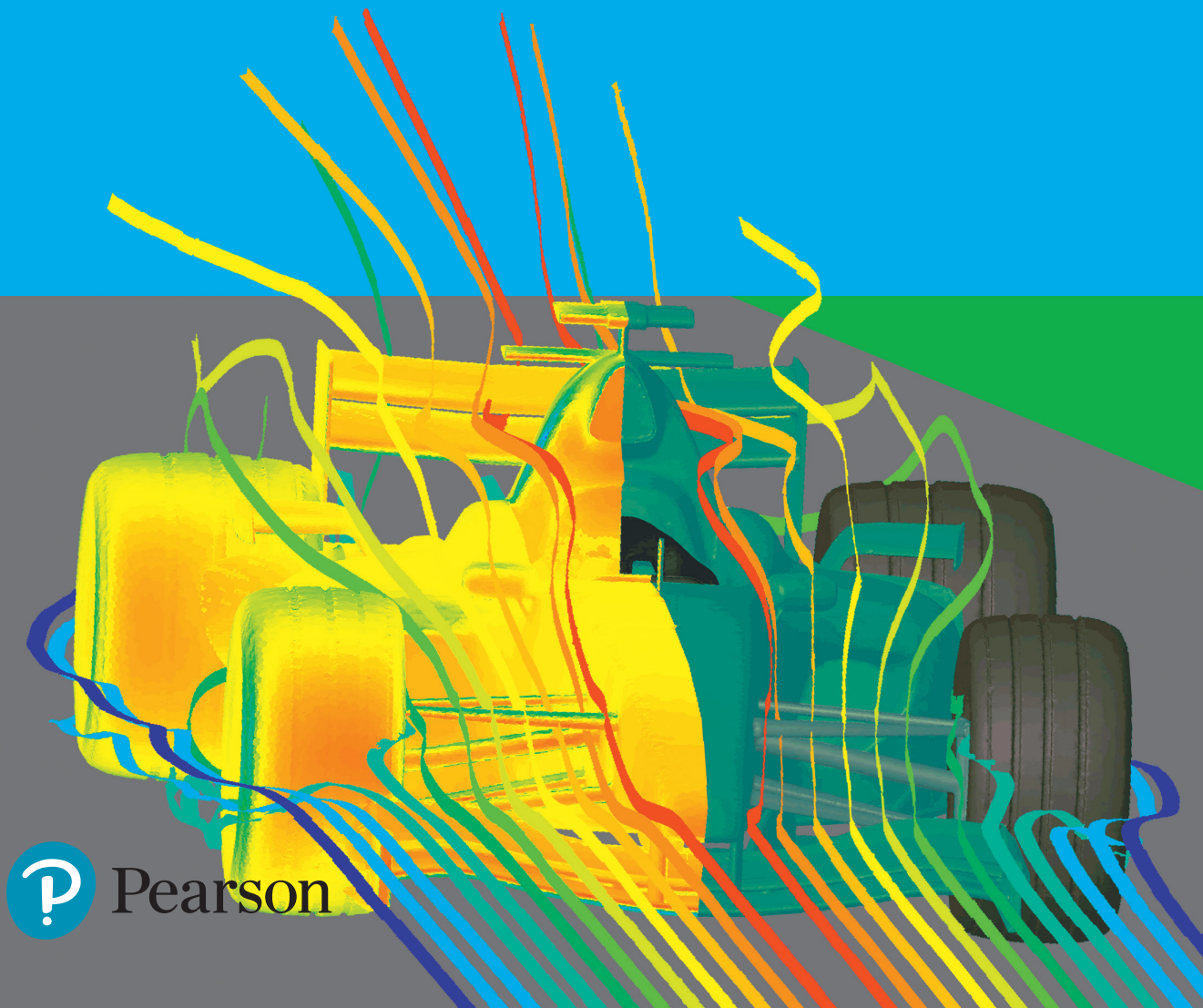


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An Introduction to  
**COMPUTATIONAL FLUID  
DYNAMICS**

The Finite Volume Method

second edition



# **An Introduction to Computational Fluid Dynamics**

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# **An Introduction to Computational Fluid Dynamics e-book**

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