

GLOBAL
EDITION



AN INTRODUCTION TO ANALYSIS

FOURTH EDITION

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An Introduction to Analysis

Introduction to Analysis, Global Edition (Classic Version)

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