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Foundation Maths

SEVENTH EDITION



Pearson

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

Foundation Maths

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