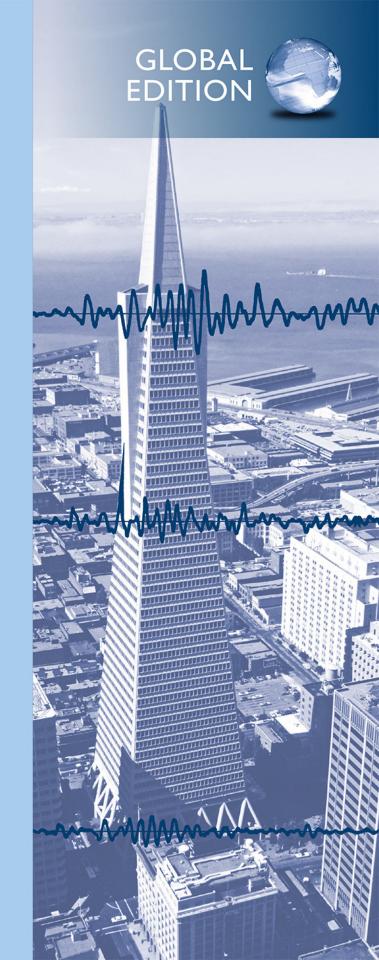
Dynamics of Structures

Theory and Applications to Earthquake Engineering

Fifth Edition in SI Units

Anil K. Chopra





DYNAMICS OF STRUCTURES

Dynamics of Structures, SI Editionv

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