

GLOBAL  
EDITION



# Fundamentals of Differential Equations

NINTH EDITION

Nagle • Saff • Snider



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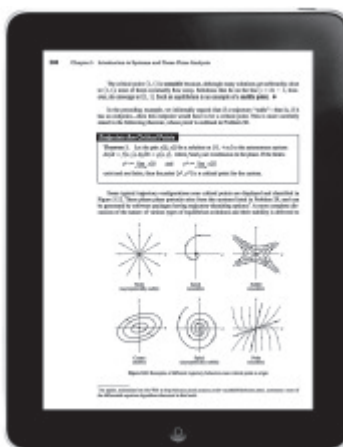


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Dedicated to R. Kent Nagle

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