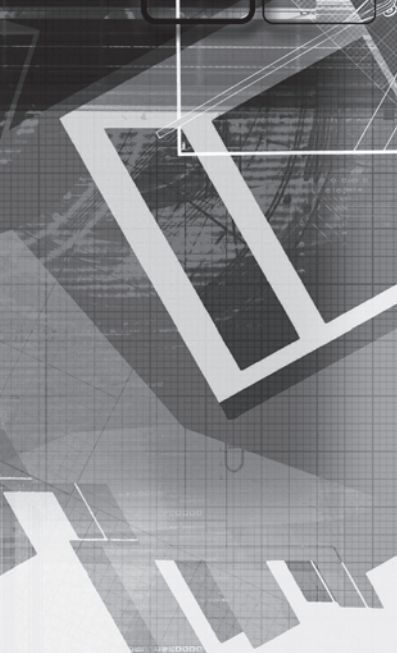


ADVANCED MODERN ENGINEERING MATHEMATICS

Fifth Edition

Glyn James & Phil Dyke



Advanced Modern Engineering Mathematics

Fifth Edition

Advanced Modern Engineering Maths

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