# ENGINEERING MATHEMATICS

A Foundation for Electronic, Electrical, Communications and Systems Engineers

FIFTH EDITION

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Pearson

# Engineering Mathematics

# Engineering Mathematics

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