

GLOBAL
EDITION



College Algebra and Trigonometry

THIRD EDITION

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College Algebra and Trigonometry

College Algebra and Trigonometry, Global Edition

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