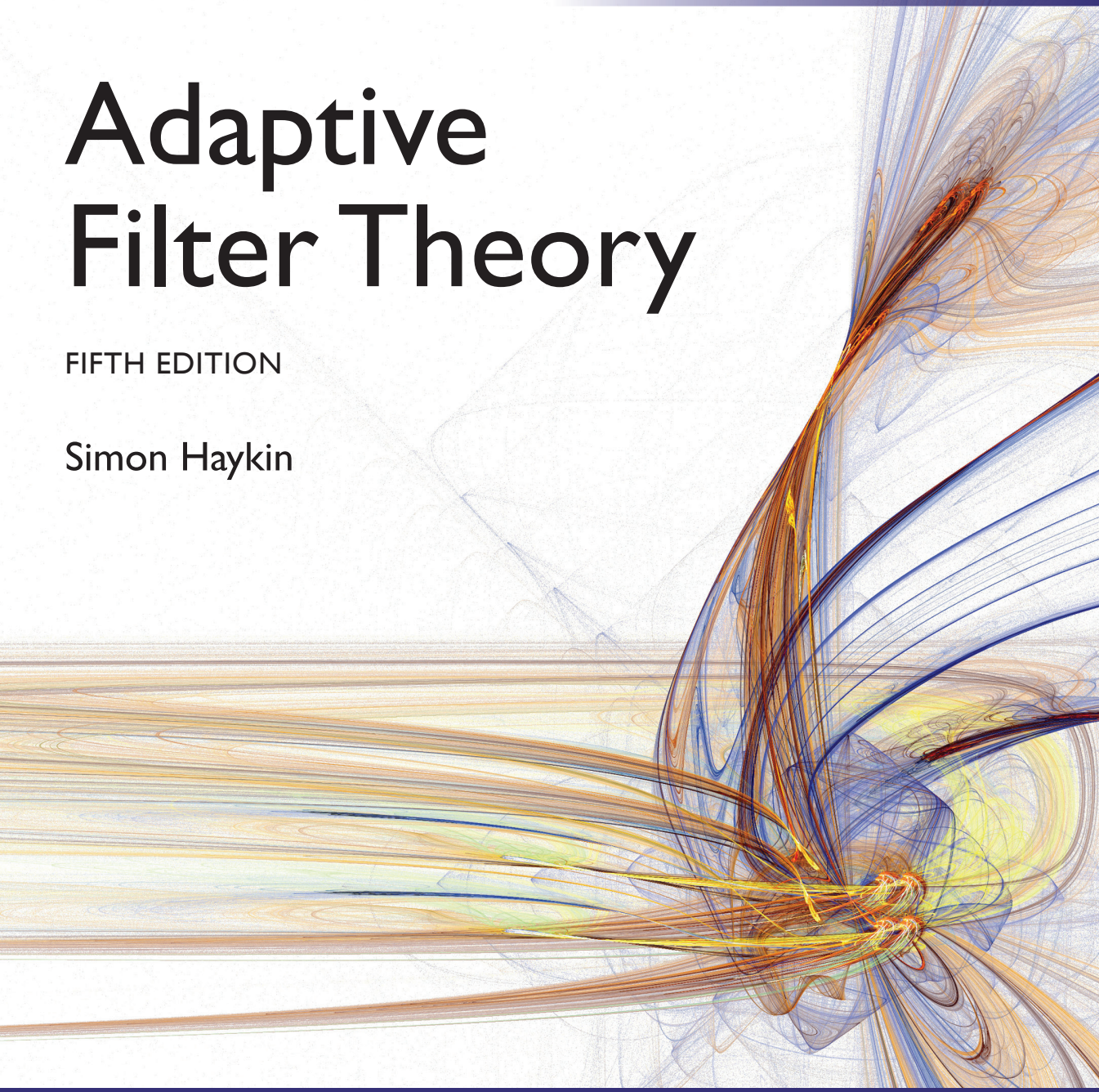
INTERNATIONAL EDITION

Adaptive Filter Theory

FIFTH EDITION

Simon Haykin



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ADAPTIVE FILTER THEORY

Fifth Edition

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