

# Finite Element Analysis

# Theory and Application with ANSYS

**FOURTH EDITION** 



**PEARSON** 

## FINITE ELEMENT ANALYSIS

## Finite Element Analysis: Theory and Application with ANSYS, Global Edition

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