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# The Art of Computer Programming

VOLUME 4

Constraint Satisfaction

FASCICLE

7

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DONALD E. KNUTH

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# THE ART OF COMPUTER PROGRAMMING

VOLUME 4, FASCICLE 7

## Constraint Satisfaction

DONALD E. KNUTH *Stanford University*



**ADDISON-WESLEY**

Hoboken, New Jersey

# Art of Computer Programming, Volume 4, Fascicle 7, The: Constraint Satisfaction

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