

COMPUTER GRAPHICS

PRINCIPLES AND PRACTICE

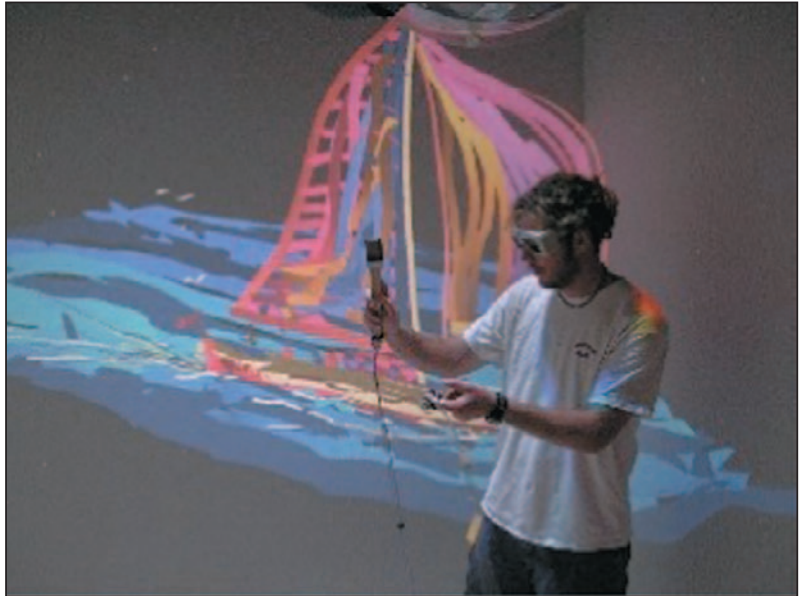
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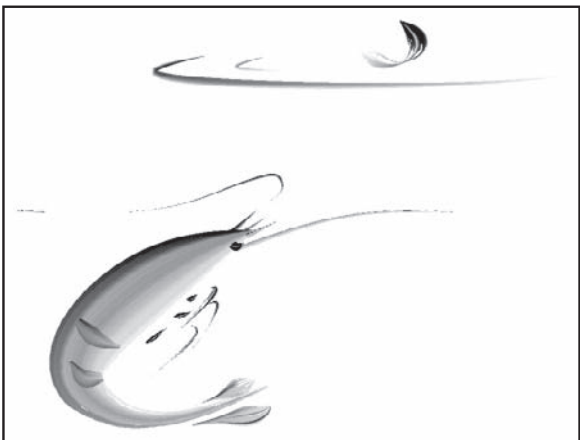
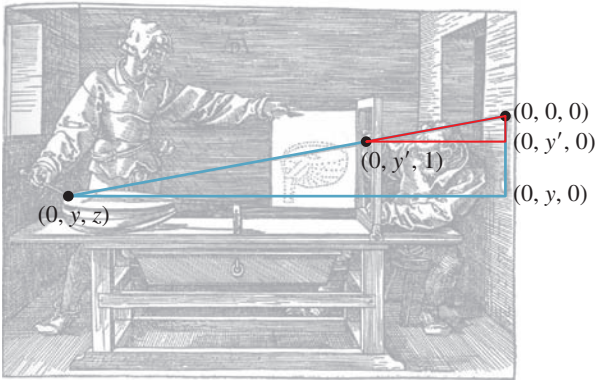
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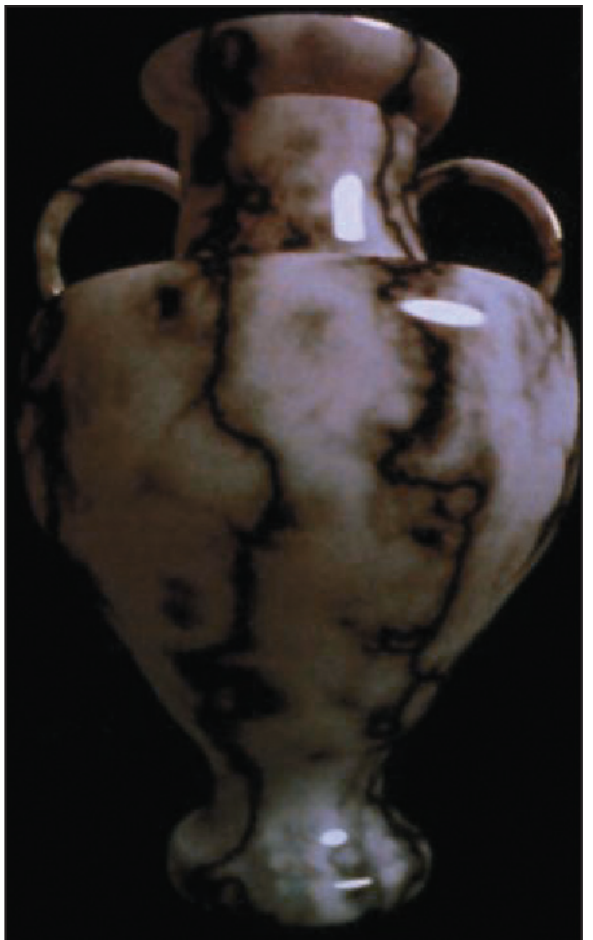
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Computer Graphics: Principles and Practice

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