

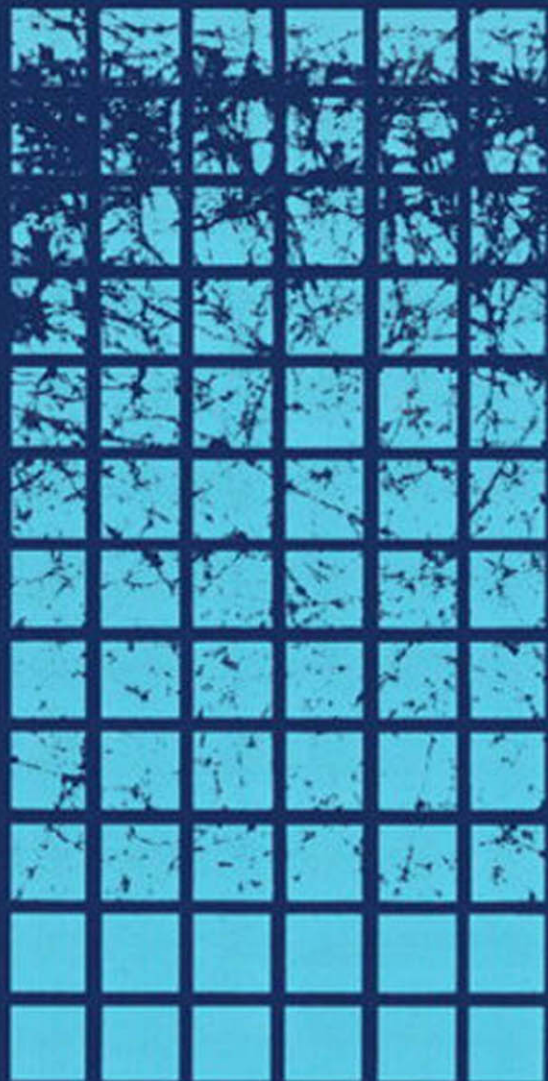
INFORMATION AND SYSTEM SCIENCES SERIES  
Thomas Kailath, Series Editor

# SYSTEM IDENTIFICATION

*second edition*

Theory  
FOR THE  
User

LENNART  
LJUNG



# System Identification

## Theory for the User

Second Edition



# System Identification: Theory for the User

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